## Teacher's Manual

## instruction

# Mathematics 

## Dear Educator,

Instruction Coach has been built to meet the new, higher standards for mathematics and contains the rigor that your students will need. We believe you will find it to be an excellent resource for comprehensive instruction, practice, and assessment.

## The Triumph Learning Team

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## Instructional Overview

## Welcome to Instruction Coach!

This program is based on the philosophy that mathematical skills are built on concepts. Math, more than any other school subject, builds from concept to concept, one on top of another, over several years. When students understand concepts and how they connect to skills, they are better equipped to solve the problems that they encounter in the real world.

## Implementation

This program is your instructional anchor. You probably have other instructional materials in your classthey may be books and workbooks, computers, smart boards, pads, math manipulatives, or a basal textbook. You know when and how to apply the appropriate mix of instruction for your students as the content demands. In the end, these are your students, who are in your class and your school. You know your class best. You have the wisdom and knowledge to use this program in the best way possible for your students.

## Supplemental Implementation

If you use a basal textbook, then this program becomes an excellent partner in helping to strengthen and advance your mathematics instruction. This program and your basal can work together hand in hand; whether for lesson review, lesson practice, chapter review, or working through a performance task, this program is ready to help your students.

The flexibility of this program allows it to fit into many stages of instruction. For example, you may want to use this program on a twice-weekly basis to add depth, understanding, and practice to the basal experience. Alternatively, you may choose to use this program at the end of a chapter of instruction if you judge that your students need additional practice in that chapter. You can then choose several or all lessons from the chapter to reinforce and review concepts and skills included in that chapter. Or, you may want to assign specific lessons from this program to groups of students or to individuals.

## Basal Implementation

This program offers complete instruction for your grade. It combines complete instruction with an accompanying Teacher's Manual full of practical and inventive suggestions for every lesson. You can use it as your main instructional vehicle throughout the school year because it is a complete package- from instructional lessons to robust lesson practice to chapter reviews to performance tasks. A friendly HomeSchool Connection booklet brings extra practice to the student's home and informs families of the math that children are learning.

## Student Book

## Lessons

The Lessons flow in a logical fashion, building on prior knowledge from the forerunner chapter or from a chapter whose content links to the chapter at hand. Lessons will often take several days to complete. Lessons work through many variants of the skills and/or concepts. All skills are developed through Examples. The interactive Examples in the lessons stimulate discussions, allow groups of students to interact and answer questions, and connect with other parts of the math curriculum.

At the end of all Examples, interactive sections have students complete the problem posed in the Example. Each lesson includes an Example that is aligned to mathematical practices. Suggestions for how to use the Example to develop deeper understanding are addressed in the lesson plan.

The Try feature provides a scaffolded example for children to work through individually or as a class before they are assigned practice.


Practice appears in each lesson. Each lesson concludes with practice aligned to the content covered in the instruction. The practice items build in difficulty and offer a variety of question types.

Each Practice section ends with a problem that stretches and extends the skill(s) in the lesson. Many of the lesson Practice sections include a Talk About It feature as well. Young children may not be able to write too much - a number or a word here, a sentence there - but they can surely talk when encouraged. By means of the built-in Talk About It feature, children can tell how they get their answers, tell why a solution works, and even argue why their answer is better than someone else's. The trick is to encourage conversation about math questions and to stimulate reasoning and thinking. Talk About lt is a starter for good conversations about math questions; and when successful, the conversations induce good mathematical practices. Look for them, extend them, and then create your own Talk About Its.


## Chapter Reviews

Chapter Reviews consist of questions that cover all standards in the domain. Chapter Reviews include multiple-choice questions, short-answer questions, and extendedresponse questions. These reviews serve as excellent assessment tools. Each Chapter Review ends with a problem that stretches and extends the skill(s) in the lessons.

Chapter 4 Review
Write how many sides and angles. Name the shape.

sides

angles


3 What is the name of the shape?


4 Which is a cube?


## Performance Tasks

Performance Tasks appear at the end of each Chapter Review. They complement instruction with non-routine applications of chapter skills. Performance Tasks require students to perform a range of activities, from drawing and building to writing and talking about.


## Glossary and Math Tools

The Student Edition also includes a Glossary and a selection of content-specific math tools. When students encounter a highlighted term in their book, they will find this term defined in the glossary. When Math Tools are necessary for a given lesson, you will find this reference in the Materials section of your lesson plan-occasionally, these tools are referenced in the lesson itself.


## Teacher's Manual

## Lesson Progressions

The content covered in this program is organized by chapter. The content across grades 1 and 2 connects back to math taught earlier in kindergarten. This program helps you make critical connections between topics within a single grade level and across grade levels.

Lesson Progressions in the Teacher's Manual help you focus on key connections. Each Chapter includes a Lesson Progression Map that offers a visual progression of lesson content across grades, including both pre- and post-requisite lessons for each chapter. Focusing instruction on these connections will help strengthen the continuum of mathematical concepts and skills.


## Lesson Flow Charts

You will find useful Lesson Flow Charts in this manual at the beginning of each Chapter's lesson plans. These are your guides to how lessons are connected within that Chapter. You can look at an entire Chapter and make judgments about how to plan your teaching strategies.


## Lesson Plans

Lesson plans provide guidance for each student lesson.

```
Learning Objectives for each lesson are stated clearly.
```


## Problem Solving: Addition

| Vocabulary |
| :--- | :--- |
| add <br> addends <br> sum <br> equation |
| Materials |
| - counters |
| - place-value blocks (optional) |
| - Fluency Practice, page A2 |
| - Fluency Practice, page A3 |

Scripted pre-lesson activities introduce new concepts
and skills and
focus on previous knowledge.

## Learning Objective

Children will use addition to solve one- and two-step word problems with unknowns in all positions.

## Before the Lesson

In Grade 1, children have learned to use addition within 20 to solve one-step word problems. In Grade 2, they will use addition within 100 to solve one- and two-step word problems.
Tell children the following story: Tyrone bought 6 red peppers and 8 green peppers. How many peppers did he buy in all?
Ask: What can you do to find how many peppers he bought in all? You can count all the peppers. Say: When you find how many in all, you are adding Counting can help you add.

Use 6 red counters and 8 yellow counters. Show a red counter. Say: Let's use red counters to show the number of red peppers Tyrone bought. Ask: How many red peppers did he buy? 6 How many red counters should we use for the red peppers? 6 Display 6 red counters.
Show a yellow counter. Say: Let's use yellow counters to show the number of green peppers Tyrone bought. Ask: How many green peppers did he buy? 8 How many yellow counters should you use
for the green peppers? 8 Place 8 yellow counters to the right of the red ones with a space between the red and yellow ones.


Ask: How can we find how many there are in all? Put them together and count. Have children count to find the sum. Ask: How many peppers are there in all? 14
Say: An addition sentence shows what happens when we add two numbers. Write the parts of the addition sentence $6+8=14$ on the board as you say the following: The addition sentence begins with the number of red peppers Tyrone bought. Then a plus sign shows that you will add the number of green peppers Tyrone bought. Ask: How many green peppers did Tyrone buy? 8 Say: So we need to write 8. Next we need to write an equal sign. Ask: What does the equal sign mean? Whatever is on one side of the sign has the same value as what is


## Lesson Plans (continued)

Say: Look at the drawing. The addends have been joined together to make the sum. Ask: Which addend do we know? 63 What does 63 stand for? Liam's stamps What is the sum? 83 What does 83 stand for? The number of stamps in all What do we need to find? The addend that stands for the number of stamps Kayla has
Then ask: When you start with the addend you know, 63 , and add 10, what is the sum? 73 Does this number match the sum? No Add 10 more to 73. What is the sum? 83 Does this match the sum? Yes How many did we add? 20 Children should trace over the dotted 20 in the box. Direct children's attention to the statement below. Have them fill in the answer.

Kayla has $\mathbf{2 0}$ stamps.

## Example 5

The problem in this example requires more than one step to solve. To make this clear to children, the problem is stepped out. Read the problem with the class.

For Step 1, ask: How can we find how many blocks Austin had at the start? By adding 12 and 3 or by counting on three from 12 How many blocks in all does Austin have at the start? 15 Children should trace over the dotted 15 in the box.
For Step 2, ask: What do we need to find? How many blocks Austin's dad gave him How many blocks does Austin have now? 45 How can we find how many blocks his dad gave him? By adding on tens to 15 until we reach a sum of 45 ; then we count how many tens we had to add.

Guide children through adding 10s to get from 15 to 45. Ask: How many blocks did Austin's dad give him? 30 blocks Children should trace over the dotted 30 in the triangle. Finally, ask: Austin's dad gave him how many blocks? 30 Direct children's attention to the statement below. Have them fill in the answer.

Austin's dad gave him 30 blocks.
You might like to explore this topic further by asking children to use place-value models to display this problem. Ask: How could you model Step 1 of this problem? Step 1 could be modeled with 1 ten and 2 ones to stand for the 12 blue blocks and 3 ones to stand for the 3 red blocks. That's a sum of 15 in all.

Ask: How could you model Step 2 of this problem? Step 2 could be modeled by adding 1 ten to the 5 for a total of 25 , adding another ten to the 25 for a total of 35 , and adding one more ten to the 35 to reach the total of 45 .

## Try

Place-value blocks are used to model this problem Children are given two addends, for which they need to find the sum.
Ask: How many puzzle pieces does Maya have? 27 Say: The problem tells us that Jason has 50 more pieces than Maya. Ask: What do we need to find? How many pieces Jason has How do the models help you to solve this problem? They help me to count on tens.

Ask: How many tens will you count on? 5 Why 5 tens? Because 50 is equal to 5 tens Say: Let's start at 27 and count on 50. 27 (pause) 37, 47, 57, 67, 77 Have children trace the 37 and write the other numbers they counted. Ask: How many puzzle pieces does Jason have? 77 Children should write 77 in the box to complete the equation $27+50=$

Jason has 77 puzzle pieces.
To further explore this topic, replace the numbers in this problem with other numbers. Say, for example: suppose Maya has 37 puzzle pieces. And suppose ason has 60 more puzzle pieces than Maya. How many puzzle pieces does Jason have? 97 Allow children to use place-value blocks to model the problems.

## Practice

For this section, children will count on or add to find either a missing addend or a sum. As they work, check to be sure that they understand how to approach problems 4 and 5, each of which requires a two-step solution.

For answers, see page 150.
SOIVE For problem 5, children are asked to write and solve an equation to determine how many stamps Lauren has in all. After children write the equation to describe the situation, you may wish to ask them to use place-value models to explain how they solved the problem.

Full support in working through instruction with scripting

TRY page presents a problem with scaffolding to guide students.

## Chapter Openers

Chapter Openers are the opening acts of each Chapter. They explore, entertain, and prepare students for the Chapter ahead. Openers, in the form of high-interest art, set the stage for the lessons and standards of the Chapter by addressing the math coming up. Each Chapter Opener is a different setting and story. Although this manual provides guidance about how you might approach Chapter Openers, you should use your own story-telling capabilities to expand on what you find here. Designed to be engaging and fun, they should be good ways to organize the new Chapter.


## Appendix A: Fluency Practice

Fluency Practice appears at the end of the Teacher's Manual. The Teacher's Manual includes practice pages that are specially designed to align with fluencies. Instructions on when and how to administer the fluency pages are included in the lesson plans within this manual.


## Appendix B: Check-Ups

How will you assess student progress in this program? The answer is here in the Teacher's Manual in the form of a series called Check-Ups. These are questions that you can use as you best see fit- with a small group, with an individual student, or with a full class. Use them for diagnosis or for formative assessment. Each Check-Up assesses a single Chapter-the natural scope for diagnosis or formative assessment-where you may want to check up on how your students are doing above and beyond their daily interaction with lessons and lesson practice. While a Chapter Review should also be seen as an opportunity to look at an entire domain of content, the CheckUps also provide information about student mastery. The questions are easy to implement either by paper and pencil, or verbally-thus allowing for informal assessment. All you have to do is make as many copies from this manual as you need.


## Home-School Connection

The Home-School Connection booklet keeps math alive beyond the time constraints of the school day and the walls of the school building. The Home-School Connection booklet provides a short sample of what is happening in each lesson in the form of the last question or two of each lesson's Practice section. You will find that these questions are not exact replicas of those questions; the numbers and sometimes the forms have changed slightly to offer a repeat of the same types of questions. By using these questions, children can review the content of their school lessons with their care-givers. In this way, children extend their thinking about math, thus deepening their understanding and preparation for the next day.


## Lesson

# 2 <br> <br> Problem Solving: Subtraction 

 <br> <br> Problem Solving: Subtraction}

## Learning Objective

- Children will use subtraction to solve one- and two-step word problems with unknowns in all positions.

| Vocabulary |
| :--- |
| subtract <br> difference |

## Materials

- place-value blocks (optional)
- Fluency Practice, page A4
- Fluency Practice, page A5


## Before the Lesson

In Grade 1, children learned to solve word problems by subtracting within 20. In Grade 2, they will use subtraction within 100 to solve one- and two-step word problems.
Tell the children the following story: A man is selling fruit. He had 12 apples. He sells 7 of the apples. How many apples does he have left?

Say: You can use a drawing to show this problem.
Ask: How many apples does the man start with? 12 So, how many apples should we draw to start? 12 Draw 12 apples on the board or call a volunteer to do it.

Ask: How many apples does he sell? 7 What should you do to show that he sells 7? Take 7 away. Explain that in a drawing, they can put an $X$ on an object to show that it is being taken away. Cross off 7 apples, one at a time, or call a volunteer to do it, as the class counts with you. 1, 2, 3, 4, 5, 6, 7


Ask: How many apples are left? Have children count with you the apples that are not crossed off. 1, 2, 3, 4, 5

Say: You can subtract to solve this problem. Write the parts of the subtraction sentence $12-7=5$ on the board as you say the following: The subtraction sentence will begin with the number of apples that the man had. Ask: How many apples did he start with? 12 Then we need to put a minus sign to show that we will take away the number of apples he sells. Ask: How many apples does he sell? 7 Say: So we need to write 7. Next we will need an equal sign. Ask: How many apples does he have left? 5 Say: So we need to write 5. We read this sentence as twelve minus seven equals five.
4 You might want to use Fluency Practice pages A4 and A5 to help children review subtraction for sums to 10.

## Teaching the Lesson

This lesson has children solve word problems by using subtraction. They will use subtraction sentences to represent word problems that have missing numbers in all positions. Have children turn to page 14.

## Example 1

Explain that this problem asks them to take apart a group and that they can use a subtraction to solve the problem.

Ask: How many stickers are there? 19 How many stickers are blue? 8 How can we find how many stickers are yellow? Subtract What should we subtract? 19 - 8

Point out that the box in the subtraction sentence stands for the missing number, in this case, the number of yellow stickers. Ask: What is 19 minus 8? 11 Children should trace the dotted 11. Direct children's attention to the statement below. Read it with the class and have them fill in the answer.

There are 11 yellow stickers.

## Example 2

This example presents a problem in which the original number of objects in a group is given and the number of objects that have been taken away from the group is also given. Children need to find how many are left.
Ask: How many acorns did the squirrel have at first? 20 How many acorns did the squirrel eat? 5 What do we need to find? How many acorns were left
Say: 20 stands for the number of acorns in all. Ask: How many acorns are crossed out? 5 Ask: What do the 5 that are crossed out represent? The number of acorns that the squirrel ate Say: We can say that we are subtracting the 5 acorns from a group of 20.

Ask: How can we find the number of acorns that are left? Count the acorns that are not crossed out; subtract Have children trace over the dotted 15 in the box. Direct children's attention to the statement below and have them write in the answer.
There were 15 acorns left.

## Example 3

In this example, the number being taken away is the missing number.

Ask: How many pennies did Blake start with? 70 How many pennies did Blake end up with? 30 How can we find how many pennies Blake spent? Subtract What subtraction sentence should we use? 70 minus $\square$ equals 30.
Direct attention to the place-value blocks. Ask: How many tens are there in all? 7 How many of Blake's pennies does each ten represent? 10 pennies Then ask: How many pennies do all 7 tens represent? 70 pennies
Ask: How many tens do the 30 pennies that are left stand for? 3 tens If each ten stands for 10 pennies, how many pennies do these 3 tens represent? 30 pennies
Ask: What does it say below the 4 tens? Pennies spent What does that mean? It means that Blake spent 4 tens, or 40 pennies. Have children trace over the dotted 40 in the box. Ask: How many pennies did Blake spend? 40

Blake spent 40 pennies.

## Example 4

This example shows a subtraction problem that has a missing starting number (minuend).
Ask: How many walnuts did Sharon eat? 10 How many walnuts are left? 24 What do we need to find? How many walnuts were on the table to start Say: We can use a subtraction sentence because some walnuts were taken away.

Say: We do not know the number of walnuts on the table to start, so we do not know the first number in our sentence. We will use a box for the unknown number in our equation. Ask: Do we know how many walnuts Sharon ate? Yes How many walnuts did Sharon eat? 10 Say: We can write minus 10 for the walnuts Sharon ate. Ask: How many walnuts were left? 24
Say: We have 24 left and 10 were eaten. One way to solve this is to take the 24 walnuts that were left and add back the 10 that were eaten. Ask: $24+10$ equals what number? 34 What number minus 10 equals 24? 34 Children should trace the dotted 34. Have the children complete the sentence below.
There were 34 walnuts on the table to start.

Common Error Make sure that children do not subtract the 10 from the 24 that are left. They should understand that they are looking for the total number of walnuts that were on the table before some were eaten.

You may wish to have children compare this problem to the missing-addend problem, Example 4, in Lesson 1. Ask: How is Example 4 in Lesson 1 like Example 4 in this lesson? Both use an addend-addend-sum chart. Ask: How do the two problems differ? For Example 4 in Lesson 1, we needed to find an addend. For this example, we needed to find a sum.

## Example 5

For this example, children use place-value models and subtract tens in order to solve a word problem involving comparing.
Ask: What do we know about the number of games Luke has? That Luke has 20 fewer games than MaryJo has How many games does Mary-Jo have? 50 What do we need to find to solve this problem? How many games Luke has
Ask: What equation can we write to show this problem? $50-20=\quad$ What does the model show? 5 tens with 2 tens crossed out Finally, ask: How many tens are left? 3 What is the value of 3 tens? 30
Ask: How many games does Luke have? 30 Have children trace over the dotted 30 . Then draw children's attention to the statement below and have them write in the answer.

Luke has $\mathbf{3 0}$ games.

## Example 6

This example involves a two-step word problem. Step 1 requires children to find a sum. Step 2 has them find the difference between that sum and another number. Read the problem with the class.

For Step 1, ask: How many storybooks did Haley have at the start? 18 How many animal books did she have? 3 How many books does Haley have after she gives some of these books away? 19 What do we need to find to solve this problem? How many books Haley gave away
For Step 1, ask:What can we do to find how many books Haley had before she gave some away? We
can count on 3 ones from 18. Say: Let's count on 3 from 18. 18 (pause), 19, 20, 21 Ask: What is the last number you will say? Twenty-one Children should trace over the dotted 21 in the box. Ask: How many books did Haley have at the start? 21

For Step 2, ask: Now, what do we need to find? How many books Haley gave away What subtraction equation helps us find this? $21-\Delta=19$ How can we find the missing number? By using a related addition sentence and counting on from 19, the number of books Haley has now, until we reach 21, the number of books she had at the start.

Say: Let's count on together from nineteen: 19 (pause), 20, 21 Ask: How many did we count on from 19 to 21? 2 So, how many of her 21 books did Haley give away? 2 Children should trace over the dotted 2 in the triangle. Then direct their attention to the statement below and have them write in the answer.

Haley gave away 2 books.

## Try

This problem uses place-value blocks to model the subtraction needed to solve the word problem.
Read the problem with the class. Ask: How many coins does Lucy have? 30 fewer than Gavin has How many coins does Gavin have? 80 What do we need to find? The number of coins that Lucy has How will we go about finding the number of coins Lucy has? We will subtract 30 from 80 .
Ask: What does the first model show? It shows 8 tens. What do the 8 tens stand for? The 80 coins that Gavin has What does the second model show? 3 of the 8 tens crossed out Explain that the 3 tens are crossed out to show that Lucy has 3 tens, or 30, fewer coins than Gavin. Ask: How many tens are left after 3 tens are crossed out? 5 What is the value of the 5 tens? 50
Finally, ask: How many coins does Lucy have? 50 Children should trace over the dotted 50 in the box to complete the equation $80-30=50$ and then write the answer in the statement below.
Lucy has 30 coins.

To further explore this topic, have children explain why they needed to subtract to solve this problem. Ask: Why did you subtract, and not add, to solve this problem? Possible answer: The problem said that Gavin has 80 coins and Lucy has 30 fewer. If I added, I would have found that Lucy has more than 80 coins, which doesn't match the problem.

## Practice

As children work, pay special attention to problem 2. Be sure they understand that they need to find how many toys were in the attic at the start of the
problem. You may have them use place-value blocks to model the problem. Help them read the equation as, "What number minus twenty equals thirty-three?"

For answers, see page 150.
SOIVE To challenge children to express their understanding of problem 5, you may want to have them use the existing problem as the basis of a problem of their own by replacing the names and numbers in the problem with names and numbers of their choosing. Again, have them write and solve equations for such problems.

